

The Explaining of “Magic” Nuclear Numbers by a Quasi-Crystalline Nuclear Model, of Possible Cold Genesis

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Abstract. The paper is based on a cold genesis theory of the author, (CGT), in which the proton results as formed by a neutral N^p cluster of degenerate electrons and an attached positron with degenerate spin and magnetic moment. Also, the neutron results in a “dynamide” model, as formed by a proton and a degenerate electron with degenerate spin and magnetic moment, with its centroid incorporated in the proton quantum volume and rotated around the proton center.

In the paper it is shown that the stable nuclei with “magic” or semi-“magic” number of protons or and neutrons: 2; 8; 20; 28; (32, 36, 40); 50; 82; 126, are retrieved by a quasi-crystalline nuclear model of ground state $T \rightarrow 0K$, as sum of quasi-crystalline forms with integer number of alpha particles with $2n^2$ protons and $4n^2$ nucleons having small deformation parameter, for the double 'magic' nuclei. This possibility may be explained by the dynamide model of neutron of CGT by the hypothesis of α^0 -neutron clusters cold forming at $T \rightarrow 0K$ and the generating of small square forms of neutral α^0 -particles which are transformed into nuclei by α^0 -particles transforming into α^+ and α^{2+} particles which attract new α^0 -particles, the process being repeated until the forming of double magic nuclei which may attract nucleons or α^0 -clusters transformed thereafter into α^+ clusters, or of nuclei with “magic” mass number. According to the model, the nucleus $^{208}Pb_{82}$ corresponds to the initial form: $^{208}N_{104}$ ($Z=2(4^2+6^2)$) in which 22 attracted α^0 -clusters were transformed into α^+ clusters, by β^- radiation emission.

The proposed model predicts that the nuclei with $A=4(5^2+7^2)=296$, $A=4 \times (6^2+2 \times 4^2+2 \times 2^2)=304$ nucleons and $Z=114+120$ are more stable in the ground state than the forms: 114/184, 120/182 predicted with the “nuclear shells” model. Also, it results as possible the forming of cold semi-“magic” nuclei with hexagonal symmetry, with the mass number $A=\Sigma(3 \times 4n^2)$, ($n=1...5$).

Keywords: crystalline nuclear model, magic nuclei, dynamide neutron model, tetra-neutron, cold genesis

1 Introduction

- In a Cold Genesis Theory of Matter and Fields of the author, (CGT-[1-4]), based on the Galilean relativity [6], the discovered elementary particles are explained by a vortexial model, of composite fermion type, as Bose –Einstein Condensate of N^p gammons considered as thermalized pairs: $\gamma^* = (e^-e^+)$ of axially coupled electrons with opposed charges which became degenerate electrons inside the neutral N^p cluster, i.e. - quasi-electrons with diminished mass, charge and magnetic moment: $m_e^* \approx 0.81m_e$; $e^* \approx (2/3)e$; $\mu_e^* \approx \mu_e(2.79m_e/m_p) \approx \mu_p$, [4,5].

The motivation of the theory results from the fact that neither the Big-Bang theory nor the quantum vacuum fluctuations theory not explain physically the generation of the specific properties of the elementary particles (mass spectrum, spin, magnetic moment, electric charge, etc.) and of the fundamental fields, even if the Standard Model of particles, the Quantum chromodynamics and the Electro-weak theory are compatible with a lot of observational data.

- The theory uses an electron model with the charge $e=S^0/k_1$ contained by its surface $S^0=4\pi a^2$ of radius: $a=1.41$ fm, (close to the value of the nucleon radius resulted from the expression of the nuclear volume: $r_r \approx 1.25 \div 1.5$ fm) and with an exponential variation of its density and of quanta density variation inside the electron's quantum volume:

$$\begin{aligned} \rho_e &= \rho_e^0 \cdot e^{-r/\eta}; (\rho_e^0 = 22.24 \text{ kg/m}^3; \eta = 0.965 \text{ fm}); \\ \rho_e(a) &= \mu_0/k_1^2 = 5.17 \times 10^{-13} \text{ kg}; (k_1 = 4\pi a^2/e) \end{aligned} \quad (1)$$

- The particle's magnetic moment μ_e^* results in CGT as etherono-quantonic vortex: $\Gamma_\mu^*(r)=\Gamma_A+\Gamma_B$, of heavy ("sinergonic") etherons ($m_s \approx 10^{-60}$ kg) - generating the magnetic potential \mathbf{A} and of quantons ($m_h = h \cdot 1/c^2 = 7.37 \times 10^{-51}$ kg) - generating vortex-tubes ξ_B that materializes the \mathbf{B} -field lines of the magnetic induction.

- The virtual radius: r_μ^a of the proton's magnetic moment, μ_p , results by a degenerate Compton radius of an attached positron, which decreases when the protonic positron is included in the neutral N^p cluster volume, from the value: $r_\mu^e = 3.86 \times 10^{-13}$ m, to the value: $r_i = r_\mu^p = 0.59$ fm, as a consequence of the increasing of the impenetrable quantum volume mean density in which is included the protonic positron's centroid, m_0 , from the value: $\bar{\rho}_e$ to the value: $\bar{\rho}_n \cong f_d N^p \cdot \bar{\rho}_e$, in which: $k_p = \bar{\rho}_n / \bar{\rho}_e$ - the gyromagnetic ratio; $\bar{\rho}_e$; $\bar{\rho}_n$ - the mean density of electron and of nucleon; f_d - the degeneration coefficient which gives the quasidelectron mass $m_e^* \approx 0.81 m_e$.

The neutral N^p -cluster of nucleons and of other astro-particles may be considered as composed by three cold formed quarks with preonic structure based on a neutral preon $z^0 \approx 34 m_e$, [1-4].

- The superposition of the (N^p+1) quantonic vortices: Γ_μ^* of the proton' quasidelectrons generates inside a volume with the radius: $r_\mu^a = 2.35$ fm [1-4] a total dynamic pressure: $P_n = (1/2) \rho_n(r) \cdot c^2$ which gives a nuclear potential: $V_n(r)$, in an Eulerian form, having a variation according to eqn.:

$$V_n(r) = v_i P_n(r) = V_n^0 \cdot e^{-r/\eta^*}; \quad V_n^0 = v_i P_n^0 = (v_i/2) \rho_n^0 \cdot c^2 \quad \text{with: } \eta^* = 0.8 \text{ fm [2],} \quad (2)$$

($v_i(r_i) \approx 0.86 \div 0.9$ fm³ - the nucleon's impenetrable quantum volume of nuclear interaction).

- Also, the neutron results in CGT by a specific "dynamide" model, with a degenerate electron with degenerate magnetic moment: $\mu_e^* \approx -4.6 \mu_N$ (μ_N - the nuclear magneton) rotated inside the quantum volume of a proton by the etherono-quantonic vortex Γ_p of the protonic magnetic moment μ_p , with a speed $v_e \approx 1.7 \times 10^{-2} c$, to an orbital with a radius: $r_e^* \approx 1.283$ fm, under dynamic equilibrium of forces on tangent and radial directions, [3-5].

There are also relative recent experiments which are in concordance with CGT, such as:

i) the possibility to "split" the gamma- quantum into a pair $e^+ - e^-$ with an electrostatic energy

$$E_e = 2m_e c^2 \quad (\text{that argues a } \gamma\text{-quantum forming as pair of degenerate electrons, } e^{*+} - e^{*-});$$

ii) the experimental obtaining of a BEC of photons, (a "super-photon"), by a German team (2010), (proving the existence of photonic rest mass);

iii) the experimental evidencing of a $34 m_e$ neutral boson, (preon of cold genesis - in CGT), by a Hungarian team, (but considered as quantum of a fifth force, of leptons to quarks binding, [6]);

iv) the almost same size order of the radius of scattering centers determined inside the electron and inside the nucleon, ($\sim 10^{-18}$ m [7] - value considered also for quarks [8], but being the radius of a super-dense electronic kernel (centroid), in CGT, [1-5]).

It is known also the opinion that the majority of the atomic elements are synthesized inside the stars, at very high temperature, for example, in a supernova explosion, in conditions in which the kinetic energy of the lightest nuclei (H, D, He) exceeds the repulsive coulombian potential and favors their fusion.

A question that arises is that at least the "magic" nuclei may be formed also "at cold" ($T \rightarrow 0$ K), as quasi-crystalline clusters of protons and neutrons.

2 The Explanation of the Nuclear "Magic" Numbers of Nuclear Stability through a Quasi-Crystalline Nuclear Model

By the solitonic "dynamide" model of neutron reconsidered in CGT [1-4] and in concordance with the observations that shown a maximum nuclear stability for even-even nuclei, the nuclear model resulted from CGT for the ground state $T \rightarrow 0$ K is of quasi-crystalline type, corresponding to the extreme-uniparticle model (of Schmidt type), to the "nuclear molecule" model, to the alpha particle cluster model and to the rotating rigid vibratory core model.

According to this quasi-crystalline model, at $T \rightarrow 0$ K the nucleus consists of symmetrical overlapping of square forms with an integer number of alpha particles, the unpaired nucleon(s) being rotated around this quasi-crystalline nucleus by the quantum vortex of the nuclear magnetic moment, which explains - according to the theory, the centrifugal nuclear potential, or being attached to the double 'magic' central part as α^0 clusters of four neutrons.

The stable nuclei with "magic" number of protons or and neutrons (the most known being: 2; 8; 20; 28; 40; 50; 82; 126) are found- according to the model, as symmetrical quasi-crystalline forms resulted from overlapping of integer number of alpha particles, with $A=\Sigma(4n^2)$ nucleons ($n=1,2,\dots,7$) and $Z=\Sigma(2n^2)$ protons- for the double magic nuclei, with relative small deformation parameter δ , (figure 1), with a total number $K_a=(1; 2; 3; 4)$, $(K_b, K_c)=(0; 1; 2)$ of squared or hexagonal forms with $n_a^2, n_b^2, n_c^2, (3n_a^2, 3n_b^2, 3n_c^2)$ α -particles on the levels a., b., c.:

Double 'magic' forms: $(Z=A/2): A=4^1, (^4\text{He}_2); A=4\times 2^2=16, (^{16}\text{O}_8); A=4\times(3^2+1^2)=40, (^{40}\text{Ca});$

$$Z=2\times(4^2+5^2)=82, A=4\times(4^2+6^2), (^{208}\text{Pb}_{82}\text{-double 'magic'}).$$

Simple 'magic' or 'semi-magic' nuclear forms: $A=4\times(3^2+2\times 1^2), (^{44}\text{Ca}\text{- stable isotope});$

$A=4\times 4\times 2^2, (^{64}\text{Zn}\text{- the most stable/abundant isotope})$

$A=4\times(3^2+2^2), (^{52}\text{Cr}\text{- stable/abundant isotope}); A=4\times(3^2+2\times 2^2)=68, (^{68}\text{Zn}\text{- stable/abundant isotope});$

$A=4\times(3^2+2^2+1^2)=56$, or $A=4\times(3\times 2^2+2\times 1^2)=56; (^{56}\text{Fe}\text{- the most stable/abundant is.});$

$A=4\times 2\times 3^2=72, (^{72}\text{Ge}\text{- stable/ab. is.}); A=4\times(2\times 3^2+2\times 1^2)=80, (^{80}\text{Kr}; ^{80}\text{Se}\text{- stable/ab. is.});$

$A=4\times(2\times 3^2+2^2+1^2)=92, (^{92}\text{Zr}\text{- stable is.}); A=4\times(4^2+2\times 2^2)=96, (^{96}\text{Mo}\text{- stable/ab. is.});$

$A=4\times 3\times 3^2=108, (^{108}\text{Pd}\text{- stable/ab.is.}); A=4\times(5^2+2^2)=116, (^{116}\text{Sn}\text{ (}Z=2\cdot 5^2=50\text{)}\text{- stable/ab. is.});$

$A=4\times 2\times 4^2, (^{128}\text{Xe}\text{- stable is.}); A=4\times(4\times 3^2+2\times 1^2)=152, (^{152}\text{Sm}, (Z=62)\text{- the most ab. is.});$

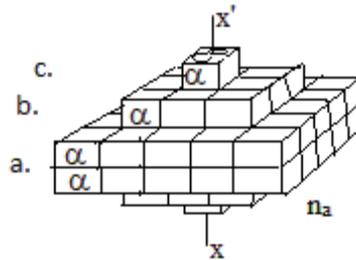


Figure 1. "Magic" form of a quasi-crystal nucleus

For Ge, Zr, Kr, Sn, etc., the greater number of neutrons ($N>Z$) may be explained in the model by the attraction of some neutron α^0 -clusters or 1+3 excess neutrons in the nuclear field of a double magic core, at $T\rightarrow 0$, these neutrons or α^0 -clusters remaining un-transformed or generating a nuclear quasi-crystalline form with "magic" mass number, $A=\Sigma(4n^2)$, in which some neutral α^0 -clusters are only partially transformed into α^{1+} -clusters.

For example, ^{116}Sn may be in a quasi-crystalline form: $A=4\times 5^2+4\times 4$, i.e.- a double magic form with $Z=2\times 5^2$ and four symmetrically attached α^0 -clusters. Also, ^{80}Kr (stable isotope, $A=4\times(2\times 3^2+2\times 1^2)=80$), may be considered as formed by a double 'magic' quasi-crystalline form with $Z=2\times 2\times 3^2$ and two symmetrically attached α^0 -clusters.

The fact that the nuclei such as ^{40}Ca , ^{52}Cr , ^{56}Fe , ^{72}Ge , ^{80}Se , ^{152}Sm , ^{108}Pd , are the most abundant isotopes is explained by the conclusion that it results as quasi-crystalline forms in the ground state.

The fact that the stable isotope $^{90}\text{Zr}_{40}$ (with 'magic' Z and N) is the most abundant is explained by the conclusion that it resulted from the quasi-crystalline form ^{92}Zr ($N=52$ -also stable/abundant isotope) by the losing of two corner neutrons at higher nuclear temperature, being explained the fact that $N=50$ was found also as 'magic' number of neutrons [9], in this case.

The "magic" form of the nucleus $^{208}\text{Pb}_{82}$ corresponds -according to the model, to an initial double "magic" quasi-crystalline form: $^{208}\text{N}_{104}$, ($A=4\times(4^2+6^2)$) in which 22 protons were transformed into neutrons with beta emission, giving $Z=82$.

Similarly can be formed a nucleus with $A=4(5^2+7^2)=296$ nucleons, with $Z=114\div 120$, (close to the predicted (quasi)stable form: 114/298 predicted with the "nuclear shells" model, [9]). The nucleus with $A=296$ ($Z=119; 120$) was experimentally obtained by the reactions:



Other 'magic' nuclei may be explained by the model in a similar way:

- The double magic nucleus ^{48}Ca may be considered as composed by 3 square forms with $2^2=4$ α -particles:

$$A=4\times(3\times 2^2)=48, \quad \text{in which 4 protons were transformed into neutrons;}$$

- The double magic nucleus ^{56}Ni may be considered as composed by 3 square forms with $2^2=4$ α -particles and one α -particle on each side: $A=4\times(3\times 2^2+2\times 1^2)=56$;
- The double magic nucleus $^{96}\text{Zr}_{40}$ may be derived from quasi-crystalline square forms of 24 alpha particles:

$$A=4\times(4^2+2\times 2^2)=96,$$

in which 8 protons were transformed into neutrons by electrons "capturing" or by β^+ disintegration.

Other stable nuclei which may be explained by the proposed quasi-crystalline model are:

- The nucleus with $A=4\times(2\times 4^2+2\times 2^2)=160$; (Dysprosium: ^{160}Dy –stable isotope);
- The nucleus with $A=4\times(5^2+2\times 3^2)=172$; (Yttrium: ^{172}Yt - stable isotope);
- The nucleus with $A=4\times(5^2+2\times 3^2+2\times 1^2)=180$; (^{180}Hf ($Z=72$) –stable isotope);

Similarly may result as more stable than the adjacent isotopes, the nuclear forms:

- $A=272=4\times(6^2+2\times 4^2)=4\times(2\times 5^2+2\times 3^2)$: ^{272}Bh (Bohrium, $t_{1/2}=11\text{s}$ -close to Hassium 270, considered double magic in the form: $Z=108$; $N=162$);
- $A=4\times(2\times 5^2+2\times 3^2+2\times 1^2)=280$; (Rg–Roentgenium, which decays with α -particles emission).

Based on the calculation of pairing gap, two neutron separation energy and the shell correction energy, M. Bhuyan, S. Patra and Ahmad found $Z=120$ as the next proton magic number and $N=172, 182/184, 208$ and 258 as the subsequent neutron magic numbers, [10].

Also, Biswal, Bhuyan et al.,[11], based on a newly developed approach, of simple effective interaction, found that the combination of magic nucleus occurs at $N=182$ ($Z=114, 120, 126$), predicting a long half-life for $^{292}120$ and $^{304}120$, [12].

According to the quasi-crystalline model, it result as 'magic' at $T\rightarrow 0$ the nuclei with $A=304$, corresponding to $Z=120$, $N=184$ and with $A=296$, corresponding to $Z=114$, $N=182$, in the quasi-crystalline forms:

$$A=4\times(6^2+2\times 4^2+2\times 2^2)=304 \text{ (Unb) and } A=4\times(7^2+5^2)=296$$

The nucleus ^{304}Unb , (Unbilinium) was obtained by the reactions:



A higher stability of the nucleus with $A=296$ was deducted also by other authors [13], in the form: $Z=112$, $N=184$, in concordance with recent experiments [14] which gave evidence of the significant increase of the stability of heavy nuclei approaching the magic number $N=184$.

The fact that – at ordinary temperatures, the nuclei with $A>210$ are generally unstable may indicate either that their real nuclear structure is in accordance with the 'drop' nuclear model, resulted by the rearranging of the nucleons at a specific nuclear temperature $T\approx 10^9\div 10^{11}$ K which can 'melt' the initial quasi-crystalline form, or in a vibrational quasi-crystalline state, at a nuclear temperature close to the solid-liquid transition temperature, T_n .

This last possibility is in concordance with the fact that a quasi-crystalline nuclear structure was evidenced by experiments of particle dispersion on heavy cores, (W.Bauer, [15]).

The concordance with the model of alpha-particles cluster type explains also the fact that the decay of the experimentally obtained nuclei, with $Z\geq 95$ ($A\geq 243$), is generally produced by α -particles emission.

Similarly may be formed- according to the model, a nucleus with:

$$A=4(7^2+2\times 5^2)=396; \quad A=4\times(2\times 6^2+2\times 4^2)=416; \quad A=4\times(2\times 6^2+2\times 4^2+2\times 2^2)=448;$$

$$A=4\times(7^2+2\times 5^2+2\times 3^2)=468; \quad A=4\times(2\times 7^2+2\times 5^2+2\times 3^2)=517;$$

Nucleons or alpha-weakly-linked particles formed from valence nucleons may be rotated around the nuclear quasi-crystalline core (Lonnroth, [16]), particularly- as in the extreme- uniparticle model (Schmidt, [17]) by the action of the quantum vortex Γ_μ of the nuclear magnetic moment μ_N (according to the quantum-vortexial nature of the magnetic field, considered in CGT [1-4]) which explains also the nuclear centrifugal potential.

3 The Explaining of the Nuclear Fission of a Quasi-Crystalline Nucleus by CGT

The nuclear fission of a quasi-crystalline nucleus may be explained in CGT by a deuteron self-resonance mechanism which generates a decrease in the value of the interaction potential V_n between nucleons by nucleonic vibrations in portions with incompleteness of the quasi-crystalline nucleonic network or with

excess nucleons, as consequence of a higher vibration liberty of the nucleons of this nuclear part, according to CGT [1-4].

This mechanism and the energy of the interaction particle (neutron) determine a local change of the quasi-crystalline network into a quasi-liquid phase. This transition is characterized in the nuclear physics by the 'quantality' parameter Λ introduced by B. Mottelson [18]:

$$\Lambda = 2(b_0/r_0)^2 = \hbar^2/m_n r_0^2 V_0 \quad (5)$$

in which: r_0 – the inter-particles distance; m_n – the nucleon mass; V_0 – the typical magnitude of the inter-constituents interaction.

The parameter Λ is defined as the ratio of the zero-point kinetic energy of the confined particle to its potential energy. The liquid phase corresponds to $\Lambda > 0.1$, whereas the crystalline solid phase is characterized by values of $\Lambda < 0.1$, [19]. In the case of nuclei, using $V_0 \approx 100 \text{ MeV}$ and $r_0 \approx 1 \text{ fm}$ – in accordance with the Reid potential, it results $\Lambda \approx 0.5$.

The model also explains the super-asymmetric nuclear fission [20] by the conclusion that the incompleteness of the quasi-crystalline network or a number of excess nucleons leads to a higher 'vibration liberty' l_v of these weakly bound nucleons and this vibration decreases the value of the scalar nucleonic potential and determines either the nucleus fission into sub-nuclei with symmetrical quasi-crystalline forms (often - "magical" or quasi-stable forms), or gamma vibration spectra, as a result of the self-resonance of less strongly bound nucleons, according to a spin-dependent nuclear potential relation (CGT, [1-4]):

$$V_s^n(r) = V_s^l \cdot e^{-\frac{r}{\eta^*}} = V_s^0 \cdot e^{-\frac{l_v}{\eta^*}} \cdot e^{-\frac{r}{\eta^*}} \quad [\text{MeV}]; \quad l_v^* = l_v^0 \cdot \left(\frac{3}{2} - \frac{1}{2} \bar{\tau}_p \cdot \bar{\tau}_n\right); \quad \bar{\tau} = \frac{\bar{s}_n}{s_n}; \quad (6)$$

in which: $V_s^0 = 109.8 \text{ MeV}$; $\eta^* = 0.8 \text{ fm}$, [2], $l_v \cong A_v$, (the vibration amplitude);

$$l_v^0(E_v) \cong 1 \text{ fm - for deuteron; } (l_v(E_v=0)=0); \quad l_v \sim E_v = \frac{1}{2} m_n v_n^2 = \frac{1}{2} k_v \cdot A_v^2$$

The relation (6) corresponds also to the generalized nuclear model by the conclusion that the vibration energy of the nucleons: $\epsilon_v \sim r^2$ decreases the value of the nuclear potential well: V_s^1 .

The degeneration of the nucleonic potential through the nucleon's vibration, according to eqn. (6), may explain also the transformation mechanism of the compound nucleus by interaction with low energy particles up to 2 MeV, as in the case of the Be9 nucleus that can be transformed with a gamma quantum of only 1.78 MeV, even if the binding energy given by the sum of its nucleons is $\sim 58 \text{ MeV}$. Some reactions with thermal neutrons (of several tens of eV) can also be explained as in the case of the reaction of a light Be8 compound nucleus forming:

- $\text{Li7} + \text{H1} \rightarrow \text{Be8} \rightarrow 2\text{He4} + \gamma$ - generated with only 125 eV proton energy, in which Be8 emits an electromagnetic γ radiation of 17 MeV, or of type (n; α) like in the reaction:
- $\text{B10} + \text{n} \rightarrow \text{Li7} + \alpha$, generated with thermal neutrons (of few eV) even if normally there are necessary neutrons with the energy of 0.5...10 MeV, [21].

Other exo-energetic nuclear reactions produced at low energies of interaction particles, which sustains the conclusion of CGT regarding the decrease of the scalar potential of the nucleons with relatively small vibration energies, are:

- ${}^2\text{H} + {}^2\text{H} \rightarrow {}^3\text{He} + \text{n}$; $Q = 3.25 \text{ MeV}$;
- ${}^2\text{H} + {}^3\text{H} \rightarrow {}^4\text{He} + \text{n}$; $Q = 17.6 \text{ MeV}$

in which the resulting neutron energy is 2, 5 and 14 MeV respectively and the energy of the incident deuterons may be below 1 MeV, for example: 0.1 MeV, as in the case d).

According to the model, is explained- by the relation (6) and the self-resonance mechanism of the deuteronic systems, also the emission of a smaller nucleus by a compound nucleus excited with interaction particles of only 1÷2 MeV after a time of about $10^{-15} \div 10^{-15}$ seconds, (much longer than the nuclear interaction time: $\sim 10^{-22} \text{ s}$.), in nuclear reactions such as:

$${}^{27}\text{Al} + \text{p} \rightarrow {}^{24}\text{Mg} + \alpha; \quad {}^4\text{He} + {}^{14}\text{N} \rightarrow {}^{18}\text{F}^* \rightarrow {}^{17}\text{F} + \text{n} \quad (7)$$

The quasi-crystalline model is in concordance also with the vibrated rigid rotator (of Schmidt type, with the unpaired nucleon generating the spin and the magnetic moment of the nucleus) and with the experiments of alpha-particles scattering on heavy cores, which revealed a nuclear behavior according to a quasi-crystalline nuclear model, (V. Ershov, Alma-Ata [22]).

The correspondence of the nuclear binding energy value experimentally determined with the value resulted by the Weizsäcker's relation [23] which considers a "drop" nuclear model, may be explained by

the proposed quasi-crystalline model by the conclusion that- at the nuclear temperature T_n of solid→liquid transition ($\Lambda > 0.1$) induced by the interaction energy with an atomic particle, the nucleons vibrations determines a decreasing of the binding energy according to eqn. (6) and a re-arranging of the nucleons in a more spherically symmetric way, corresponding to a viscous “liquid” phase.

4 The Possibility of a Cold Genesis of Quasi-Crystalline Nuclei

A possible explanation of the concordance of the nuclear 'magicity' with the quasi-crystalline nuclear model could be the 'cold' producing of atomic nuclei in the beginning of the Universe' forming, from neutral clusters of four neutrons: $\alpha^0 = 4n^0$, (“tetra-neutron”), the nuclei being formed by beta transformation of at most a half of neutrons into protons during the formation of square forms of neutral α^0 - clusters and the addition of new α^0 -clusters, this process generating initially small square forms with $2^2\alpha^0$ particles in which the neutral α^0 - particles are transformed into double charged α^{2+} -particles, attracting thereafter new α^0 -particles, the process being repeated until the forming of double magic nuclei with $Z = \Sigma(2n^2)$, $A = \Sigma(4n^2)$, which may attract excess nucleons or α^0 - clusters which are partially transformed thereafter into α^+ - clusters.

This cold genesis scenario is, sustainable through a neutron-type "dynamide" model, with partially included negatron in the proton quantum volume (CGT [1-4]), by the fact that -if the neutrons may be formed at $T \rightarrow 0K$ by a cold gas of protons and electrons and the neutron's stability is increased with the temperature decreasing, the impulse of the formed neutrons may be enough low for be favored the forming of a Bose-Einstein condensate, if the density of neutrons is enough high for the producing of quantum effects, (i.e. - if the thermal de Broglie wavelength: $\lambda_t = \hbar / \sqrt{2mk_b T}$ becomes comparable with the average inter-particle spacing).

In 2016, physicists working at the RIKEN nuclear-physics lab in Japan found evidence for the tetra-neutron forming in an experiment that involved “firing” neutron-rich helium-8 nuclei at a helium-4 target [24]. The theoretical calculations indicated a larger energy width than that measured at RIKEN, corresponding to a shorter lifetime [25].

The possibility of neutrons forming instead of hydrogen atoms forming at $T \rightarrow 0K$ is indirectly sustained also by the experiments of atomic Bose-Einstein condensate collapsing [26] which evidenced a remnant condensate as fraction of the initial condensate and the disappearing of a part of the collapsed BEC. We may suppose logically that the missing part of atoms is explained by the atomic electrons coupling, with the forming of Cooper pairs and their falling to the nucleus, with the transforming of the nuclear protons into neutrons and the releasing of neutral α^0 -clusters.

According to the model, at a temperature close to 0K, the nucleons can be formed from protons and electrons captured and incorporated into the proton quantum volume, according to the reaction:



with a lifetime higher than that observed at ordinary temperatures (about 15 minutes).

If the neutron's transformation results as in case of the “dynamide” model of CGT, by the neutron's self-resonance given by the oscillation of the neutron negatron' kernel in report with the proton center's position [2-5], we may suppose that- at very low temperature $T \rightarrow 0K$, the neutron' negatrons e^* remains attached to the proton's volume p^+ and the α^0 -clusters remain un-transformed until their mutual impact, their coupling resulting as possible by the nuclear force.

In this way they can form quadratic neutral clusters $\alpha^0 = 4n^0$ by collisions at low energy, the protonic centers of the α^0 - clusters being linked both by nuclear and magnetic forces, with antiparallel magnetic moments. Also, they are electrically and magnetically coupled with one or two electrons (magnetically coupled negatrons, forming a Cooper pair) positioned in the middle of the square shape $\alpha^0 = 4n^0$, the other two neutronic negatrons being located diametrically opposed to the Cooper pair of negatrons. These marginal electrons can be relatively readily "lost" in the form of beta radiation (β^-) by electrostatic repulsion between them and similar negatrons of other clusters $\alpha^0 = 4n^0$ with which they come in contact and by vibrations of deuteronic self-resonance. In this way, the clusters α^0 generating square forms $A_i = N^2\alpha^0$ are transformed into α^+ - particles, in a time at most equal to the life of the free neutron, ($\tau \leq \tau_n \approx 15$ min.).

The resulted square forms of α^+ -particles: $A^+=N^2\alpha^+$ or $A^+=2N^2\alpha^+$, (doublet), attracts new neutron clusters $\alpha^0=4n^0$ which generates two new square forms $A^0(n)=n^2\alpha^0$, ($n \leq N$), of dimension equal to or lower than the initial one ($A^0_i(N)$) and positioned to its square faces.

The process can be repeated with the formation of new square forms $A^0(n')$, ($n' \leq n$), which then are converted into $A^+(n')$ forms.

The ratio N/Z of nuclear stability is given according to the semi-empiric Weizsäcker's relation of the nuclear binding energy [23], in the form:

$$N/Z \approx 1 + (a_c/2a_A) \cdot A^{2/3} \tag{9}$$

in which: $a_c \approx 0.711$; $a_A = 23.7$.

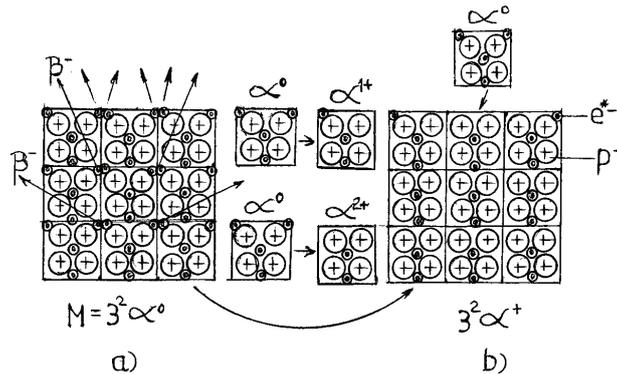


Figure 2. The forming of a nuclear quasi-crystalline form of α^0 -clusters by the forming of a first square form of α^0 -clusters a) and its transforming into a nuclear square form b)

The dependence of the a_c -coefficient on the Coulomb interaction between protons and on the number $A^{2/3}$ of nucleons positioned in the nuclear surface indicates that the excess of neutrons relative to the number of protons increases with the number of nucleons in the surface of the nucleus.

For the nuclei with $N/Z > 1$ and “magic” A-number, the relation (9) can be explained by the neutron "dynamide" model by the conclusion that a higher positive nuclear charge determines the retaining of peripheral neutronic electrons in the attracted clusters α^0 with a probability $P \sim Z$, these α^0 -clusters being only partially transformed into α^{2+} particles, (partially being transformed into α^{1+} -particles), a constant number $C_0 \sim (a_c/2a_A)$ of α^{1+} - clusters with the neutrons/protons ratio $n/z = 3/1$ being maintained in the nuclear surface unit- phenomenon which generates a mean ratio: $r_s = n_s/z_s > 1$. For the nuclei with $N/Z > 1$, the conclusion of the explicative model is that the excess neutrons are only in the nuclear surface.

For the nuclei with “magic” A- number, if K_1^α and K_2^α represent the number of nuclear clusters α^{2+} and of α^{1+} -clusters in the nuclear surface, K_2^α results by a rewritten form of the relation (9):

$$N/Z = (2K_1^\alpha + 3K_2^\alpha) / (2K_1^\alpha + K_2^\alpha) \approx 1 + 2K_2^\alpha / Z = 1 + (a_c/2a_A) \cdot A^{2/3}, \tag{10}$$

$$K_2^\alpha = (a_c/4a_A) \cdot A^{2/3} \cdot Z, \tag{11}$$

in accordance with the explanatory conclusions of the K_2^α -number's dependence on the nuclear surface and on the nuclear charge Z .

The rotation of the nucleus takes place according to the relation of Aage Bohr:

$$E_{rot} = (p^2/2J) = \hbar^2 I(I+1)/2J \tag{12}$$

where p is the angular momentum, J is the moment of inertia and I is the quantum number of the angular momentum, which is an integer for a nucleus with an even number of nucleons and an integer plus a half unit for a nucleus with an odd number of nucleons.

For the nuclei with $N/Z > 1$ and “magic” Z- number, the excess nucleons are rotated – at least in part, around the double magic kernel with $N = Z$, in accordance also with the generalized nuclear model. The property of ‘inert kernel’ with quasi-null magnetic moment of the quasi-crystal nuclear form is explained by the anti-parallel coupling of the nucleonic magnetic moments in the component α -particles.

The proposed model not exclude the possibility of other quasi-crystalline semi-“magic” nuclear clusters forming, with triangular symmetry, cold formed as neutral clusters of $t^0=3$ neutrons, transformed later into t^+ clusters (tritium clusters), such as:

${}^6\text{Li}$, ($A=2\times 3$)- stable isotope; ${}^9\text{Be}$, ($A=3\times 3$)- the most stable/abundant isotope, or as triangles with 10 nucleons, in the ground state:

${}^{20}\text{Ne}$, ($A=2\times(4+3+2+1)$)- the most stable/ abundant isotope, or with pentagonal symmetry, with $n\times 5\times 10$ nucleons, for example:

${}^{100}\text{Ru}$ (stable/abundant isotope); ${}^{150}\text{Sm}$ -stable/ab. isotope; ${}^{200}\text{Hg}$ - stable/abundant isotope. and with hexagonal symmetry, with a stability close to those of the quasi-crystalline forms with tetragonal symmetry and depending also on the nucleus deformability, the initial α^0 -clusters having a rhomboidal form inside a nuclear hexagonal form, in this case (figure 3).

The mass number A of a hexagonal quasi-crystalline nuclear form results by the relation:

$$A=\Sigma(3\times 4\times n^2); (n=1, 2\dots 5) \quad (13)$$

$n=1 \Rightarrow K_a=1, A=12$, (${}^{12}\text{C}$ -the most stable/ab. is.); $K_a=2, A=24$, (${}^{24}\text{Mg}$ -the most stable/ab. is.)

$n=2 \Rightarrow A=48$, (${}^{48}\text{Ti}$ -the most stable isotope); $K_a=2, A=84$, (${}^{84}\text{Kr}$ - the most stable/ab. is.);

$K_a=3, A=132$, (${}^{132}\text{Xe}$ -the most stable/ab. is.); $K_a=4, A=180$, (${}^{180}\text{Hf}$ -the most stable/ab. is.);

$n=3 \Rightarrow A=108$, (${}^{108}\text{Pd}$ -stable isotope); $n=4 \Rightarrow A=192$, (${}^{192}\text{Os}$ -stable isotope);

$A=(2\times 3\times 4\times 1^2+3\times 4\times 2^2)=72$, (${}^{72}\text{Ge}$ -the most stable/ab. isotope);

$A=(2\times 3\times 4\times 1^2+2\times 3\times 4\times 2^2)=120$, (${}^{120}\text{Sn}$ -the most stable/ab. isotope);

$A=(2\times 3\times 4\times 2^2+3\times 4\times 3^2)=204$, (${}^{204}\text{Pb}$ -stable isotope);

$n=5 \Rightarrow A=300$ (${}^{300}\text{Ununhexium}$); $A=3\times 4\times 4^2+2\times 3\times 4\times 3^2=408$ (?)

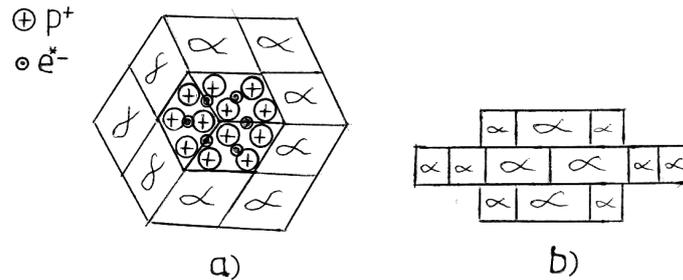


Figure 3. The forming of a quasi-crystalline nucleus from hexagonal forms of α -clusters; (${}^{72}\text{Ge}$)

The total binding energy of a quasi-crystalline nucleus may be expressed by an equation of Bethe–Weizsäcker type with the difference that the surface term: $V_s=\sigma_s\cdot S_a=a_s A^{2/3}$, ($a_s\approx 17.8\text{MeV}$) is given by the specific quasi-crystalline form of the nucleus, in the form: $V_s'=\sigma'\cdot S_q$, the volume term being: $V_v'=a_v'\cdot A$ with $a_v'\geq a_v\approx 15.75\text{MeV}$.

Because $\sigma=(1/2)F_1/l$, (force rectangular of unit length), it seems logical to have for V_s : $\sigma\approx a_v/4\pi r_0^2$, ($r_0\approx(1.2\div 1.25)\text{fm}$ - the nucleon's radius resulted from the nuclear radius expression: $R_n\approx r_0\cdot A^{1/3}$).

The fact that a_s is higher than a_v in the Weizsäcker's formula indicates either a higher value of S_a than those resulted from the 'drop' model or a higher vibration energy of the nucleons in the S_a -surface than that of the internal nucleons, or both situations.

For a 'magic' or semi-magic quasi-crystalline form, the nuclear mass and the S_a -surface may be calculated by considering three crystalline levels: a., b. and c. of squared or hexagonal forms of α -particles on each upper or lower part of the nucleus (fig. 1), with a number: n_a^2 , n_b^2 and n_c^2 of α -particles on each level of squared forms (and $3n_a^2$, $3n_b^2$ and $3n_c^2$ for each hexagonal form), n_a , n_b and n_c being the number of α -particles on the side length l_q of the squared or hexagonal form:

$$M_q^s=m_\alpha\cdot(K_a\cdot n_a^2+K_b\cdot n_b^2+K_c\cdot n_c^2); M_q^h=m_\alpha\cdot 3(K_a\cdot n_a^2+K_b\cdot n_b^2+K_c\cdot n_c^2) \quad (14)$$

with: $K_a=(1; 2; 3)$, $(K_b, K_c)=(0; 1; 2)$ - the total number of squared or hexagonal forms on the levels a., b., c. and:

$$S_a=S_a^u+S_a^l=s_\alpha\cdot 2n_a^2+\frac{1}{2}(s_\alpha)\cdot 4(K_a\cdot n_a+K_b\cdot n_b+K_c\cdot n_c)=s_\alpha\cdot 2(n_a^2+K_a\cdot n_a+K_b\cdot n_b+K_c\cdot n_c) \quad (15)$$

(s_α -the surface of the α -particle), for a nucleus formed by quasi-crystalline squared forms and:

$$S_q = S_q^u + S_q^l = s_{\alpha} \cdot 6n_a^2 + \frac{1}{2}(s_{\alpha}) \cdot 6(K_a \cdot n_a + K_b \cdot n_b + K_c \cdot n_c) = s_{\alpha} \cdot 3(2n_a^2 + K_a \cdot n_a + K_b \cdot n_b + K_c \cdot n_c) \quad (16)$$

for a nucleus formed by quasi-crystalline hexagonal forms, with S_q^u – the (upper +lower) surface, S_q^l – the lateral surface (geometrically considered, taking of two times the surface of corner nucleons).

The most stable quasi-crystalline forms are those with the high close to the side length value l_n and with double symmetry, i.e. –in report with a symmetry axis $x-x'$, when $[(n_a - n_b); (n_b - n_c)] = 2k$, ($k=1, 2, \dots$) and in report with a symmetry plane P rectangular to the $x-x'$ axis.

For example, for ^{280}Rg , $A = 4 \times (2 \times 5^2 + 2 \times 3^2 + 2 \times 1^2) = 280$ and:

$$S_q = s_{\alpha} \cdot 2(5^2 + 2 \times 5 + 2 \times 3 + 2 \times 1) = s_{\alpha} \cdot A_s = s_{\alpha} \cdot 86,$$

approximating that: $s_{\alpha} \approx 4s_n = 4\pi r_0^2$ with $r_0 \approx (1.2 \div 1.25)$ fm, with $\sigma_s = a_s / 4\pi r_0^2 = 1.03 \text{ MeV/fm}^2$ and $R_n = r_0 A^{1/3}$ – the nucleus' radius, it results that:

$$V_s = 4\pi r_0^2 A^{2/3} \sigma_s = s_{\alpha} \cdot A^{2/3} \sigma_s = 4\pi R_n^2 \sigma_s = S_n \cdot \sigma_s; V_s' = \sigma' \cdot S_q = s_{\alpha} \cdot A_s \cdot \sigma'; \quad (17)$$

For a quasi-crystal state, at the solid \rightarrow liquid transition, characterized by a mean vibration energy ϵ_v^0 of the nucleons, according to the model we may approximate that $a_v'(\epsilon_v^0) \approx a_v$ and:

$$\sigma_s'(\epsilon_v^0) = f_v^0 \cdot \sigma_a' \approx f_v^0 \cdot a_v / 4\pi r_0^2 = f_v^0 \cdot \sigma_a = f_v^0 \cdot k_{\sigma} \cdot \sigma_s; (k_{\sigma} = a_v / a_s); V_s'(\epsilon_v^0) \rightarrow V_s, \quad (18)$$

resulting that:

$$V_s / V_s' \rightarrow 1 \Rightarrow [1 / (f_v^0 \cdot k_{\sigma})] \cdot (A^{2/3} / A_s) = [1 / (f_v^0 \cdot k_{\sigma})] \cdot k_{\Lambda} \rightarrow 1; f_v^0 = f_v(\epsilon_v^0) \quad (19)$$

Conform to eqn. (19), an increased ratio k_{Λ} gives an increased binding energy, (corresponding to a lower value of $f_v^0(\epsilon_v^0)$) so a nucleus with a lower value of k_{Λ} may be 'melted' with a lower vibration energy.

For the previous case, ($A=280$) it results that: $A^{2/3}=42.8$; $A_s=86$, and $k_{\Lambda}=(A^{2/3}/A_s) \approx 0.49$.

For $A=4 \times (4 \times 3^2)=144$, (^{144}Ce - stable isotope), the quasi-crystalline nucleus has an almost cubic form, which may become spherical for $\Lambda > 0.1$, (at more intense vibrations of the nucleons), and we have:

$$A^{2/3}=27.47; S_q = s_{\alpha} \cdot A_s = s_{\alpha} \cdot (2 \times 3^2 + 2 \times 4 \times 3) = s_{\alpha} \cdot 42; (A^{2/3}/A_s) \approx 0.654.$$

The ratio $k_{\Lambda}=(A^{2/3}/A_s)$ may be considered a quasi-crystalline stability parameter.

For example, if will be extracted an α -particle from the corner of a 'magic' quasi-crystalline form:

$$4 \times (4 \times 3^2) = 144 \text{ } (^{144}\text{Ce}),$$

we will have: $A=4 \times (4 \times 3^2)=144 - \alpha=140$ (^{140}Ce - stable isotope), and:

$$A^{2/3}=26.96; S_q = s_{\alpha} \cdot A_s = s_{\alpha} \cdot (2 \times 3^2 + 2 \times 4 \times 3) = s_{\alpha} \cdot 42; (A^{2/3}/A_s) \approx 0.642 < 0.654$$

and if the α -particle is extracted from the edge, we will have:

$$S_q = s_{\alpha} \cdot A_s = s_{\alpha} \cdot (2 \times 3^2 + 2 \times 4 \times 3 + 1) = s_{\alpha} \cdot 43; (A^{2/3}/A_s) \approx 0.627 < 0.642,$$

the physical explanation being the fact that the generated hole increases the vibration liberty l_v of the adjacent remained nucleons, decreasing their binding energy, according to the relation (6).

So, by the parameter k_{Λ} it may be verified that the adding of α -particles to a 'magic' quasi-crystalline or extracting α -particles form it gives a nucleus less stable than the initial nucleus, explaining the fact that the isotopes corresponding to a complete quasi-crystalline nuclear form are generally more stable than the adjacent isotopes or at least stable isotopes.

The maintaining of the quasi-crystalline form during the nucleus forming may be explained by the conclusion that a lower vibration energy of the nucleons: $\epsilon_v < \epsilon_v^0$ permitted a higher mean value of the binding energy per nucleon, generated by a lower inter-distance between nucleons closer to the maximal value of the interaction potential ($d_i \rightarrow 0.9$ fm), in accordance with the eqn. (6) and with the criterion: $\Lambda < 0.1$ resulted by eqn. (5)).

According to eqn. (6), because the nucleons of the quasi-crystal nucleus edge have a higher vibration liberty l_v , they decrease the nucleus binding energy more than the nucleons of the upper/lower surface, in a proportion: $f_v'(\epsilon_v) \approx k_0 \cdot (S_q^l / S_q) = k_0 (A_l / A_s)$; ($A_l = S_q^l / s_{\alpha}$; $k_0(\epsilon_v) > 1$).

This assumption, resulted by the expression (6) of the nuclear potential, is in concordance with the existence of exotic nuclear reactions such as: $B10 + n \rightarrow Li7 + \alpha$ generated with thermal neutrons instead of neutrons with 0.5...10 MeV, [21] and with the fact that the vibration energy formula for nuclei with excess or lack of nucleons in report with the central completed part: $E = n \cdot \hbar \omega$, ($n=1, 2, \dots$) is correspondent to the energy formula of a quantum harmonic oscillator with the basic level: $E^0 = \hbar \omega \approx 0.3 \text{ MeV}$.

Also, we must consider a dependence of $f_v(\epsilon_v) = f_v' \cdot \Delta f_v$ on the nucleus deformation:

$$\delta_n = (l_a - h) / l_a = (2n_a - (K_a + K_b + K_c)) / 2n_a \quad (20)$$

in the semi-empiric form:

$$f_v(\epsilon_v) = f_v' \cdot \Delta f_v = K_v \cdot (A_1/A_s); \quad K_v = k_0 \cdot (1 + k_d \cdot \delta_n^2) \quad (21)$$

because a higher deformation δ_n generates- by the nucleus' ground state vibrations (oscillations in report with the initial position, perpendicular on the x-x' axis), a weakening of the F_1 -binding force between adjacent nucleons. For ^{144}Ce it results that: $\delta_n = (2 \cdot 3 - 4)/6 = 1/3$.

This assumption is in concordance with the fact that high-mass nuclei have low-lying excited states that are described as vibrations or rotations of non-spherical nuclei.

The expression of the difference $\Delta V_q = (V_v' - V_s') \geq \Delta V_n = (a_v' \cdot A - a_s \cdot A^{2/3})$ results in the approximate form:

$$\Delta V_q = (V_v' - V_s') = (a_v' \cdot A - \sigma_s' \cdot S_0) = (a_v' \cdot A - a_v' \cdot K_v \cdot A_1) \quad (22)$$

Admitting that at the solid \rightarrow liquid transition we have $a_v' \approx a_v$, ($\sigma_s' \approx f_v \cdot \sigma_n$), we may verify if the relation (21) is plausible by calculating the value of K_v in the hypothesis: $\Delta V_q(\epsilon_v^0) \approx \Delta V_n(\epsilon_v^0)$.

For heavier nuclei with quasi-crystalline form closer to a spherical form, such as ^{144}Ce , ($A = 4 \times (4 \times 3^2)$; $A_s = 42$; $A_1 = 24$), we have:

$$\Delta V_q(^{144}\text{Ce}) \approx \Delta V_n(^{144}\text{Ce}) = 1779 \text{ MeV}; \Rightarrow a_v \cdot K_v \cdot A_1 \approx a_s \cdot A^{2/3} = 489 \text{ MeV}, \quad (A_1(^{144}\text{Ce}) = 24);$$

It results the value: $K_v \approx 1.29$.

We may use the hypothesis: $a_v' \approx a_v = 15.75$, $\Delta V_q(\epsilon_v^0) \approx \Delta V_n(\epsilon_v^0)$ also for a lighter quasi-crystal nucleus: ^{72}Ge ($A = 4 \times 2 \times 3^2$), for which we have:

$$V_s = a_s \cdot A^{2/3} = 308 \text{ MeV}; \quad \Delta V_n = 826 \text{ MeV}; \quad A_1 = 12; \quad \delta_n = (2 \cdot 3 - 2)/6 = 2/3; \quad k_A = 0.57,$$

resulting the equations:

$$K_v(\text{Ce}) = k_0 \cdot (1 + k_d/3^2) \approx 1.29; \quad K_v(\text{Ge}) = k_0 \cdot (1 + 0.6^2 \cdot k_d) = 308 / (15.75 \times 12) \approx 1.629. \quad (23)$$

which gives: $k_0 = 1.177$; $k_d = 0.865$.

For the heavier nucleus ^{280}Rg ($A = 280$; $A_s = 86$; $A_1 = 36$), for which we have: $V_s = 17.8 \times 42.8 = 761.8 \text{ MeV}$; $\Delta V_n = 3648 \text{ MeV}$; $\delta_n = (2 \cdot 5 - 2 \cdot 3)/10 = 0.4$, with the resulted values we obtain:

$$V_s'(\text{Rg}) \approx a_v \cdot k_0 \cdot (1 + k_d \cdot \delta_n^2) \cdot A_1 \approx 759.7 \text{ MeV}; \quad \Delta V_q \approx 3650 \text{ MeV}, \quad \Delta V_q \text{ resulting almost equal with } \Delta V_n.$$

So the form (21) of K_v results as plausible.

If we take into account also the nuclear density lowering with the mass number A , in the form proposed by Myers and Swiatecki [27]:

$$\Delta V_n^s = \Delta V_n^0 \cdot f_I = (V_v^0 - V_s^0) \cdot f_I = (c_v \cdot A - c_s \cdot A^{2/3}) \cdot (1 - k_v I^2); \quad (24)$$

$$(f_I = (1 - k_v I^2); \quad I = (N - Z)/A; \quad c_v = 15.677; \quad c_s = 18.56; \quad k_v \approx 1.79),$$

we have: $V_s^0(\text{Ge}) = 321.2 \text{ MeV}$; $V_s^0(\text{Ce}) = 509.8 \text{ MeV}$; $V_s^0(\text{Rg}) = 794.3 \text{ MeV}$;

$$\Delta V_n^0(\text{Ge}) = 807.5 \text{ MeV}; \quad \Delta V_n^0(\text{Ce}) = 1747.6 \text{ MeV}; \quad \Delta V_n^0(\text{Rg}) = 3595.2 \text{ MeV}, \text{ and:}$$

$$K_v = k_0 \cdot (1 + k_d \cdot \delta_n^2) \leq V_s^0 / (c_v \cdot A_1) \quad (25)$$

We may calculate the value $k_0(\epsilon_v^0)$ given by a vibration energy ϵ_v^0 of nucleons characteristic to the solid \rightarrow liquid transition, using a quasi-crystal nucleus with $\delta_n \approx 0$, (close to the spherical form), such as ^{64}Zn , which has: $A = 4 \times 4 \times 2^2$; $A_1 = 2 \times (2 \times 4) = 16 = A^{2/3}$; $V_s^0(\text{Zn}) = c_s \cdot A^{2/3} = 296.9 \text{ MeV}$; $\Delta V_n^0(\text{Zn}) = 706.4 \text{ MeV}$, and for which we reconsider the approximation: $\Delta V_q(\epsilon_v^0) \approx \Delta V_n(\epsilon_v^0)$, which gives:

$$k_0(\epsilon_v^0) = k_0' \approx V_s^0 / (c_v \cdot A_1) = c_s / c_v \approx 1.1839$$

which is a plausible value because for a quasi-crystal model, we must have: $k_0(\epsilon_v^0) \leq c_s / c_v$.

We must take into account also different values for the constant k_v of eqn. (24) when the factor f_I decreases the value of V_v^0 or of V_s^0 [28]. We may use in this case, for ΔV_q , the semi-empiric form:

$$\Delta V_q = \Delta V_q^0 \cdot f_I = (V_{qv}^0 - V_{qs}^0) \cdot f_I = [c_v' \cdot A \cdot (1 - k_a I^2) - K_v \cdot c_v' \cdot A_1] \cdot f_I \approx c_v' \cdot A \cdot [1 - (k_a + k_v) \cdot I^2] - V_{qs}^0 \cdot (1 - k_v I^2) [MeV]; \quad (26)$$

$$f_I = (1 - k_v I^2); \quad I = (N - Z)/A; \quad K_v = k_0 \cdot (1 + k_d \cdot \delta_n^2); \quad \delta = (l_a - h) / l_a; \quad c_v' \geq c_v; \quad k_0(\epsilon_v^0) = c_s / c_v$$

Admitting that at the solid \rightarrow liquid transition we have $c_v' \rightarrow c_v$ and $\Delta V_q \rightarrow \Delta V_n$, we may approximate the values of the constants $k_d(\epsilon_0)$ and $k_a(\epsilon_0)$ by the hypothesis: $c_v'(\epsilon_v^0) \approx c_v$; $\Delta V_q^0 \approx \Delta V_n^0$ used for ^{72}Ge and ^{280}Rg .

With $k_0 = c_s / c_v$ we obtain the values: $k_d(\epsilon_0) = 0.9665$; $k_a(\epsilon_0) = 0.1$. With: $I^2(\text{Zn}) = 0.0039$; $I^2(\text{Ge}) = 0.01234$; $I^2(\text{Ce}) = 0.0378$; $I^2(\text{Rg}) = 0.0429$, it results:

$$\Delta V_q^0(\text{Zn}) = 706 \text{ MeV}; \quad \Delta V_n^0(\text{Ge}) = 809 \text{ MeV}; \quad \Delta V_q^0(\text{Rg}) = 3596.5 \text{ MeV};$$

- For ^{144}Ce , ($\delta_n = 1/3$), with eqn. (26) we obtain: $K_v(\text{Ce}) = k_0(1 + 0.9665 \cdot (0.3)^2) = 1.311$;

$$V_{qv}^0(\text{Ce}) = 2248.9 \text{ MeV}; \quad V_{qs}^0(\text{Ce}) = K_v \cdot c_v \cdot A_1 = 493.3 \text{ MeV}; \quad \Delta V_q^0(\text{Ce}) = 1755.6 \text{ MeV},$$

i.e.–with $\sim 0.45\%$ higher than $\Delta V_n^0(\text{Ce})=1747.6$ MeV, (obtained with eqn. (24)), as consequence of its “magic” form, given as quasi-crystal of squared forms with α^{2+} and α^+ particles with low deformation δ_n .
 - For ^{160}Dy , (stable isotope: $Z=66$; $A=4 \times (2 \times 4^2 + 2 \times 2^2)$), we have: $A_1=4 \times (4+2)=24$; $I=0.175$;

$$V_v^0(\text{Dy})=2508.3 \text{ MeV}; V_s^0(\text{Dy})=547 \text{ MeV}; \Delta V_n^0=1961.3 \text{ MeV}; \delta_n=(2 \cdot 4-4)/8=1/2;$$

$$K_v=1.47; V_{qv}^0(\text{Dy})=2500.6 \text{ MeV}; V_{qs}^0(\text{Dy})=553 \text{ MeV}; \Delta V_q^0(\text{Dy})=1947.6 \text{ MeV},$$

the value $\Delta V_q^0(\text{Dy})$ resulting with 0.7% lower than ΔV_n^0 given by eqn. (24), as consequence of a higher deformation δ_n of the quasi-crystal nucleus, which generates a higher ground state vibration of the whole nucleus.

It results that the semi-empiric expression (26) for the binding energy of the quasi-crystal nucleus gives plausible indications about the causes of the nucleus’ ‘melting’. In accordance also with the expression (5) of the ‘quantality’ parameter, it results that the nucleus can be in a quasi-crystalline state only at low vibration energies, whereas during an interaction with an atomic particle the nucleus becomes at least partially (at least in the impact zone) a quantum liquid state, by nucleons’ rearrangement, the mean value: $\sim 8\text{MeV}$ of the binding energy per nucleon –characteristic to the “drop” model, resulting by ground state vibrations of the nucleons which are higher than those of the quasi-crystal nucleus ground state, in accordance with the eqn. (26) and corresponding by eqn. (6) to a vibration liberty’ of ~ 0.8 fm in report with an initial position corresponding to an inter-distance: $r_0 \approx 1.25$ fm.

According to the model, this value of the binding energy between two adjacent nucleons may be characteristic to the nucleons of the quasi-crystal nucleus at the solid \rightarrow liquid transition temperature, when the vibration energy of the surface nucleons (mainly-those of the lateral surface, weaker bind) is transmitted to the internal nucleons.

According to the model, the quasi-crystal nucleus ‘melting’ and its transition to a ‘drop’ form is realized by an intermediary super-viscous state, in which $\delta_n \rightarrow 0$ and $k_0 \approx k_n' = c_s/c_v$, by the absorption of a specific energy: $\Delta E_T = E_q - E_n$, (E_q , E_n –the binding energy in the solid /liquid state) and by the nucleus’ dilation.

Also, it results by the model that the known vibrations spectrum of the stable nuclei with $A < 150$ resulted by surface nucleons vibrations may be specific also to a quasi-crystalline nuclear state, if the energy given by atomic vibrations at ordinary temperature is close to but lower than this ‘melting’ energy, ΔE_T .

5 Conclusions

It was shown in the paper that the stable nuclei, with “magic” or semi-“magic” number of protons or and neutrons: 2; 8; 20; 28; (32, 36, 40); 50; 82; 126, are retrieved by a quasi-crystalline nuclear model, of ground state $T \rightarrow 0\text{K}$, as symmetrical quasi-crystalline forms resulted from overlapping of integer number of alpha particles with $2n^2$ protons and $4n^2$ nucleons ($Z = \Sigma(2n^2)$; $n=1,2,\dots,7$) with a minimum deformability for the double ‘magic’ nuclei, which suggests a possible cold genesis of the nuclear matter.

The possibility of nuclear matter cold genesis may be sustained by a dynamide model of neutron resulted from a cold genesis theory, by the hypothesis of α^0 - neutron clusters cold forming, (at $T \rightarrow 0\text{K}$), by the nuclear forces, and the generating of small square forms with $n^2 \alpha^0$ particles in which the neutral α^0 -particles are transformed into charged α^+ and α^{2+} particles, attracting new α^0 -particles, the process being repeated until the forming of double magic nuclei with $Z = \Sigma(2n^2)$ which may attract excess nucleons or α^0 -clusters (transformed thereafter into α^+ clusters) or of nuclei with “magic” $A = Z + N$ number, as in the case of the nucleus $^{208}\text{Pb}_{82}$ which corresponds to the initial form: $^{208}\text{N}_{104}$ ($Z = 2(4^2 + 6^2)$) in which 22 attracted α^0 -clusters were transformed into α^+ clusters, by β^- radiation emission.

An argument in the favor of the model is the fact that the nuclei resulted as complete quasi-crystalline forms with $A = \Sigma(4n^2)$ nucleons are at least stable isotopes, the ratio: $k_A = (A^{2/3}/A_s)$ (with $A_s = S_q/s_\alpha$) being higher for these nuclei compared with their neighboring isotopes.

The proposed model predicts that the nucleus with $A = 4(5^2 + 7^2) = 296$ nucleons and $Z = 114 \div 120$ is more stable than the form: $114/184$, ($A = 298$) predicted with the “nuclear shells” model.

Also, it results as possible cold semi-“magic” nuclei with hexagonal symmetry, with $A = \Sigma(3 \times 4 \times n^2)$, ($n=1\dots 5$).

The nuclear binding energy of the quasi-crystal nucleus at the solid→liquid transition results close to the value given by the Myers and Swiatecki equation by considering its decreasing proportional not only with the nucleus' surface, but also with the ratio: (S_n^1/S_n) between the lateral and the total surface of the nucleus- as consequence of a higher vibration energy of the nucleons contained by the lateral surface and with the nucleus deformation: $\delta_n=(l_n-h)/l_n$ – as consequence of the fact that a higher deformation δ_n generates a weakening of the F_1 -binding force between adjacent nucleons by the nucleus' ground state vibrations.

It results –according to the model, that the lowering of the nucleons vibration liberty and of the nucleus' oscillation liberty increases the nuclear binding energy, this explaining also the possibility of the quasi-crystal state maintaining at very low temperatures $T\rightarrow 0K$ and the possibility of a neutron star transforming into a 'black hole' type star, at a critical mass value.

It is known also that the nuclear matter may be compressed and heated also by nuclear shock waves, mechanism which may generate the forming of multi-hyper-nuclei of Λ , Σ , Ξ , Ω - particles, according to some studies [29]. Extrapolating the resulted conclusions looking a possible cold genesis of the nuclear matter and the 'dynamide' model of neutron resulted in CGT, it results as possible also the cold forming of hyper-nuclei from positive charged and neutral hyperons (Λ^0 , Λ^+ , Σ^0 , Σ^+ , Ξ^0), with increased lifetime compared with the usual lifetime of the hyperon ($\sim 10^{-10}$ s), as consequence of the mutual strong interactions, which reduces the zeroth vibrations of the hyperons. This possibility could exist in Universe at temperatures close to 0K, at the surface of a massive or super-massive black-hole which –in this case, can grow by acquiring also hyper-nuclei, according to the model.

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